

PROGRESS TOWARDS PICOMETER ACCURACY LASER METROLOGY FOR THE SPACE INTERFEROMETRY MISSION – UPDATE FOR ICSO 2004

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ABSTRACT

The Space Interferometry Mission, scheduled for launch in 2010, is an optical stellar interferometer with a 10 meter baseline capable of micro-arcsecond accuracy astrometry. A mission-enabling technology development program conducted at JPL, has yielded the heterodyne interferometric displacement metrology gauges required for monitoring the geometry of optical components of the stellar interferometer, and for maintaining stable starlight fringes. The gauges have <20 picometer linearity, <10 micron absolute accuracy, are stable to <200 pm over the typical SIM observation periods (~1 hour), have the ability to track the motion of mirrors over several meters. We discuss the technology that led to this level of performance: low-cross-talk, low thermal coefficient optics and electronics, active optical alignment, a dual wavelength laser source, and a continuously averaging, high data rate phase measurement technique. These technologies have wide applicability and are already being used outside of the SIM project, such as by the James Webb Space telescope (JWST) and Terrestrial Planet Finder (TPF) missions.

1. INTRODUCTION

The Space Interferometry Mission (SIM) [1,2] will measure the angular positions of ~20000 astronomical objects (mainly stars) for the detection and characterization of planets, gravitational lensing events, black holes and other exotic phenomena. SIM will detect these by their influence on the angular position of the object observed. For example, an earth-sized planet orbiting a nearby star at 1 AU could be detected by the angular “wobble” of the star, about 1 μ s (=4.8 picoradians).

SIM measures the relative angles of stars on the celestial hemisphere by observing two “guide” stars which determine the orientation of SIM itself, while the third, “science” star is measured. Each star’s angular position is measured by measuring the starlight phase delay between a pair of telescopes joined in an

interferometer. Hence to function, SIM needs three starlight interferometers. (A fourth is available for redundancy.)

Metrology is needed to

1. provide knowledge of the angles between each interferometer (called external metrology) and
2. to provide internal calibration of the optical delay in the starlight interferometers (internal metrology).

Fig. 1 is a cut-away view showing the four stellar interferometers (two guide, and two science) and the external metrology beams that link them together in a three-dimensional virtual “truss” of positional information.

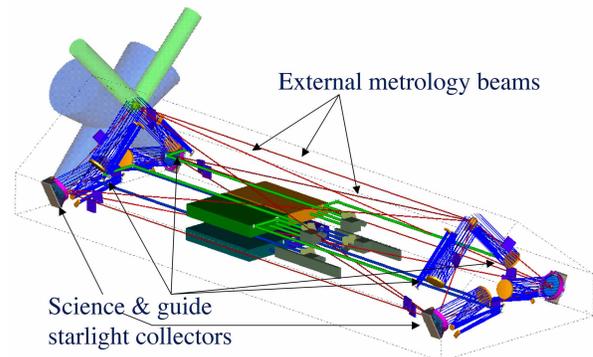


Fig. 1. SIM instrument layout. Blue indicates path of science starlight, green of guide starlight. Red indicates external metrology laser beams which measure distances between fiducials. The long dimension of the spacecraft is ~10 meters. Cones indicate the science and guide field-of-regard for the left side collectors. The right side field-of-regard cones, omitted for clarity, view the same portion of the sky.

The performance of SIM is directly related to the accuracy of the metrology. The error in measuring a star’s location is roughly $\epsilon(L)/D$ where $\epsilon(L)$ is the typical metrology error and $D=10$ meters is the baseline, the distance between the starlight interferometer telescopes. For an astrometric accuracy of 5 picoradians, we would need to limit errors to 50

pm. Because of other error sources, the contribution from metrology should actually be less than this.

Table 1. SIM metrology requirements. Number in parentheses indicate *old* requirements, as of 2000.

	Internal metrology requirement	External metrology requirement
Number of gauges	4 (8)	19 (42)
Number of gauges for mission success*	3 (6)	12 (24)
Distance between fiducials	20 m	Shortest: 2.5 m (4 m) Longest: 10.6 m (12 m)
Motion; ranges of distances	~2.6 m	~10 microns
Velocity, internal	2 cm/s while changing stars, 1 micron/sec while observing	
Accuracy (absolute)	Not needed.	3 microns rms
Accuracy relative	~57 (15) pm rms, 1 hour time scale; ~10 (8) pm rms, 90 s time scale, <i>after removal of linear component</i> **	
Temp. coefficient	2 pm/mK (soak); 50 pm/mK (sensitivity to gradients)	

* Assumes dispersed failures. Some failures are more tolerable than others.

** Modified observing schedule will allow off-line removal of drifts that are linear in time; further error removal based on instrument modeling should be possible.

Hence the metrology needs of SIM, listed in Table 1, are demanding and must be addressed for the mission to succeed. Early progress was described in the previous ICSO conference [3] and more of the real issues will be seen in another talk at this conference [4]. SIM metrology is still evolving in the laboratory and its final configuration is not yet known, but the lessons learned in ongoing experiments should apply.

It should also be noted that the accuracy requirements for a single gauge are relative to the other gauges, in the sense that if *all* gauges under/overestimate distances proportionally, the derived knowledge of the *angular shape* of SIM would be unaffected. Given that SIM's astrometric goals only require knowledge of the angles between the optical systems, to first order the need for laser source long-term wavelength stability is relaxed.

Although the distances the external metrology measures are several meters, the required dynamic range is small, a few microns, depending on the stiffness of the spacecraft.

Internal metrology has accuracy requirements similar to external metrology's but with a dynamic range of a few meters due to optical delay line motion. Because the internal metrology beam must coexist with the starlight, its aperture is constrained, causing diffraction induced errors which will be investigated by a separate experiment, the Diffraction Testbed [5].

1.1 General description of SIM metrology

Displacement metrology for the SIM testbeds (see Fig. 2) consists of a laser source [6] which supplies two $\lambda=1.3$ micron outputs with a small frequency difference F_{HET} which can be anywhere from 2 to 1000 kHz, the range of the phasemeter. The two frequency outputs serve as local oscillator (LO) and Probe sources. These outputs are carried to a metrology interferometer head (not to be confused with the *starlight* interferometers) by polarization maintaining (PM) fibers. If the experiment is inside a vacuum chamber, the fibers travel through a vacuum port to reach the metrology interferometers. The final three meters use *polarizing* fiber to remove energy from the "wrong" (fast) polarization axis before reaching the interferometers. The reason for this will be discussed later.

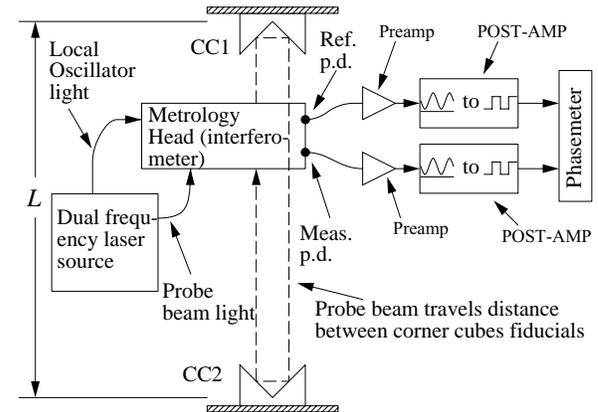


Fig. 2. Metrology gauge for measuring a single distance L . SIM uses 19 such gauges for external metrology and 4 for internal, starlight path, metrology.

Fig. 2 shows only one metrology gauge, but SIM will have 19 external gauges, which must work together to create a consistent three-dimensional shape, accurate to a few tens of picometers. The first step in showing that such a truss could be built was demonstrating close agreement between *pairs* of gauges. This was done in the Two-Gauge testbed [7], whose results are that the current gauges have

1. non-linearity < 22 pm for 10 micron displacements,

2. thermal sensitivity ~8 pm/mK,
3. drift ~300 pm/hour.

It should be noted that the cause of the drift is understood and will be corrected and that because of changes in the way the metrology data will be used, it would not be fatal to SIM even if it persisted. Similarly, we believe the thermal sensitivity can be easily reduced in the next generation of gauges.

1.2 Developments in SIM metrology

SIM metrology has evolved since the previous ICSSO conference in the following significant ways:

1. Improvement in the astrometric observing plan now allow substantial (~85% to 90%) removal of metrology drift that is linear in time. Similarly, errors that are linearly dependant on observing direction can be mostly removed in data analysis [8].
2. To reduce cyclic non-linearity, the use of polarization as a means to control probe and reference beams has been replaced with physical beam separations.
3. Active alignment of metrology beams has been successfully implemented.
4. Numerous improvements in the electronics and data processing.
5. The metrology has been scaled to various large testbeds, and has successfully been implemented as part of a SIM-like truss.

2. **IMPROVED OBSERVATION SCHEDULE AND ANALYSIS**

The order in which astrometric observations are performed has a strong impact on the required stability of the instrument. If the metrology drifts linearly with time, then by “chopping” the observations, alternately observing reference stars and science stars, the metrology error can be removed off-line.

An analogy would be having a meter stick that is growing, but also having a stable reference. We could accurately measure an unknown object with the meter stick by (1) measuring the reference then (2) measuring the unknown and (3) re-measuring the reference. If the time between measurements is constant (or at least known), then we can accurately calculate the unknown length.

In SIM’s “narrow-angle” mode [8], which will have 5 picoradian accuracy, the positions of a science star, S, and a group of 5 nearby (within 1 degree) reference stars, R₁, R₂ .. R₅, will be measured in the sequence S-R₁-S-R₂-S-R₃-S-R₄-S-R₅-S. The time between each observation will be ~90 seconds. From the data thus acquired, linear drifts (and also linear field dependencies) will be removable. Hence, the modified SIM error budget allows for linear metrology drift. Of

course, an “accelerating” drift would be problematic, and its effect must be less than 10 pm in 90 seconds.

SIM’s “wide angle mode,” accurate to 18 picoradians, is similar but with longer times scales to accommodate more targets. Within a 15 degree field of view, 6 grid (reference) stars G₁, G₂ .. G₆ will be measured, followed by N science stars S₁, S₂ .. S_N, followed by a repeated observation of the grid stars. The time scale for this sequence is ~1 hour, during which the non-linear, “accelerating,” part of metrology drift must be less than 57 pm.

These observing sequences have been incorporated into the KITE testbed which will be discussed in section 5.

3. **MINIMIZING CYCLIC ERROR**

An early obstacle to <100 pm accuracy was cyclic error, a repeating non-linearity periodic in λ/2 fiducial displacement caused by (1) leakage (crosstalk) between the L.O. and Probe beams, (2) electrical crosstalk between the Meas. and Ref. heterodyne signals and (3) computational errors arising from data age when tracking a changing distance. The RMS magnitude of the error from the first two effects may be roughly predicted [9] by the formula

$$\begin{aligned} \epsilon &= 2^{-1/2}(\lambda/2)(1/2\pi)(v/V) \\ &\approx (\lambda/18)(v/V) \end{aligned} \quad (1)$$

Applying this formula with λ=1.3 μm, we find that any leakage or crosstalk above -80 dB will cause ~10 pm cyclic error. From a practical standpoint for SIM, we strive to keep the mixing from any single source below -90 dB so that all sources taken together will be less than -80 dB.

The Two-Gauge testbed was used to confirm the cyclic performance of the gauges: after all the improvements described here, the gauges had cyclic errors that ranged from ~40 pm to <10 pm (the detection threshold). The later production metrology heads had better cyclic error performance.

3.1 Cyclic Error Due to Beam Leakage

The redesigned metrology [10,11] interferometer shown in Figures 3 and 4 represents a departure from the early SIM design (see for example [12]) in that the separation of the L.O. and Probe beams is no longer accomplished using polarizing beams splitters. Indeed, in the new design, L.O.-Probe. crosstalk is hardly an issue. However in this design, the probe beam is subdivided into an outer portion that travels between the fiducials and an inner portion that remains inside the head. These will form the Meas. and Ref. signals and any leakage (diffraction and scattering could be causes) between inner and outer beams is a potential new cause of cyclic error. Masks have been added to

reduce this leakage to acceptable levels. (The improved cyclic error of the later metrology heads was due to better diffraction blocking masks.)

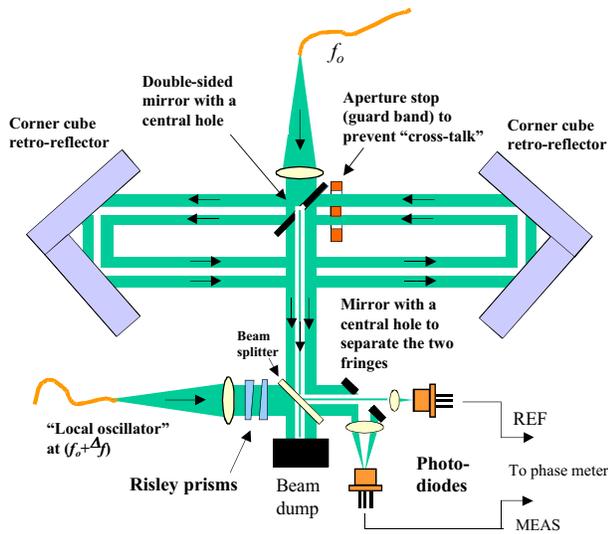


Fig. 3. Block diagram of metrology interferometer. Leakage between the outer beam, which measures distance between corner cube fiducials, and the inner beam, which acts as a reference, results in cyclic error. Similarly, crosstalk between photodiode signals causes cyclic error.

3.2 Cyclic Error Due to Multiple Gauges

As the testing of SIM metrology becomes more realistic on testbeds such as KITE (section 5) new issues inevitably arise. A new source of cyclic error has been observed that is caused by multiple gauges interrogating a common corner cube fiducial as in Fig. 6 and 7 where, for example, gauges 1, 2 and 3 all interrogate the articulated retroreflector cube. If a speck of dust scatters gauge 1's Probe beam into gauge 2, then gauge 2 will experience a cyclic error of magnitude predicted by equation 1. Better than 80 dB gauge-to-gauge isolation is required for <10 pm performance. The solution to this problem will probably involve better control of scattered light and having gauges use non-overlapping portions of the retroreflectors.

3.3 Cyclic error due to electronic crosstalk

Equation 1 also applies to signal mixing downstream of the Ref. and Meas. photodiodes. A continuing effort to upgrade the signal cabling and electronics, which will be presented elsewhere at this conference [13] is resolving this problem.

3.4 Cyclic error due to data age

This problem was noticed while testing the improved, low cyclic error, metrology gauges. It arises when fiducials are moving, and the effective time of measurement is correlated with the instantaneous phase. This effect can be removed in software as

described in [9]. It should be noted that this error and the method for its removal are specific to the phase measuring device used at JPL. For current quasi-static experiments such as KITE, the data age issue is not important but it will have to be accounted for in future testbeds, and in SIM itself, where there will be optical delay line motions to compensate for spacecraft orientation drift.

4. MINIMIZING DRIFT

Table 1 includes metrology drift requirements which, to be met, have required the use of low thermal coefficient optics and structures, and special consideration of fiber optics issues, phase measuring electronics and optical alignment.

4.1 Optical configuration for low drift

The metrology head, Figs. 3 and 4, used in SIM testbeds has evolved to the form described in [10,11] which now features

1. no polarizing optics,
2. reflective collimator optics to avoid change-of-index effects when going to vacuum,
3. monolithic zerodur optical bench,
4. zerodur and invar optical mounts.

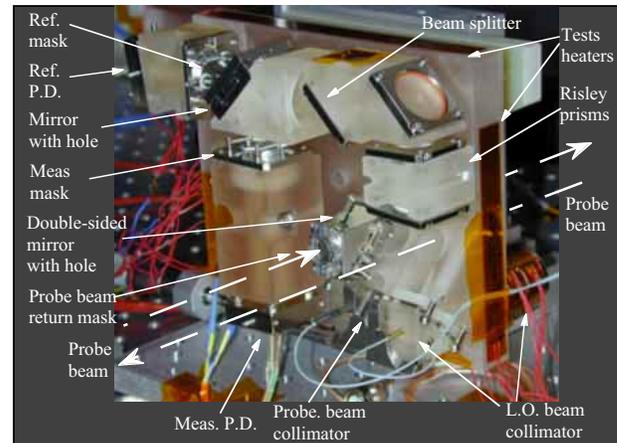


Fig. 4. Metrology head used in SIM testbeds. Heaters were placed on the rear and side surfaces of the zerodur bench supporting the optics to test thermal sensitivities.

Given this low-thermal expansion coefficient construction, we might expect a temperature sensitivity <0.1 pm/mK for uniform temperature change. Tests with the prototype in Fig 4 indicate an actual sensitivity of 7.7 pm/mK which we believe is dominated by temperature gradients. We have noticed additional drift associated with the pump-down of the test chambers which we suspect is caused by teflon rings in the area of the beam splitters and Risley prism. A third generation metrology head is currently being developed that will address this and other known flaws.

There are six gauges in KITE, and each is dithered at a different frequency (0.05 Hz separation in frequency is sufficient) to avoid cross talk. The lock-in amplifier sensor is a non-linear process, which is very sensitive to noise at the frequency of dither, transport delay and latencies in the system – these being the biggest drawbacks. However, when these drawbacks are dealt with adequately (i.e., reduce noise at dithering frequency, compensate for delay and latency) the sensor can be treated as a simple error sensor, which yields the error in pointing. The lock-in amplifier technique for KITE has been described in previous publications [14] and is not discussed here.

The pointing drift measured against a position sensitive detector is currently less than 5 micro-radians RMS/hour, with a closed loop bandwidth better than 1 Hz. Applying equation 2, this suggests the pointing drift contribution in KITE is less than 4 pm. The relatively high bandwidth allows the system to remain engaged at all times, even when large pointing errors are introduced due to routine system operation.

4.5 Absolute Metrology

At the time of the previous ICSO conference, absolute metrology for SIM was under development. This is the resolving of the half-integer wavelength ambiguity of the metrology gauges. The KITE implementation is described in [15] and results are summarized in table 2.

The desired 3 micron accuracy has proven difficult to achieve, partly because of the previously mentioned instability in the current generation of metrology heads. The new metrology heads, together with improving electronics should resolve this issue.

Table 2. Summary of current absolute metrology performance for the KITE testbed.

Two color frequency difference	15 GHz
Synthetic wavelength	2 cm
Chop rate	1 ms per color (500 Hz)
Accuracy	10 microns

5. TESTING SIM METROLOGY WITH KITE

The KITE experiment [16] is to validate the metrology truss concept that is to monitor the three-dimension shape of SIM. To simplify the problem, KITE is a two-dimensional experiment, but the lessons learned could be later transferred to the three-dimensional truss. The vertices of the retroreflectors must be co-planar (approximately horizontal) to 100 microns to allow the vertical dimension to be ignored. Currently the vertices are co-planar to ~30 microns.

Fig. 6 diagrams the KITE testbed. The metrology heads, the “quick prototype” (QP) version, measure the

distance between an articulated corner cube (ACC) and triple corner cubes (TCC) and a fixed “planarity” corner cube (PCC). The longest dimension is 2.9 meters, about 1/4th of the SIM baseline.

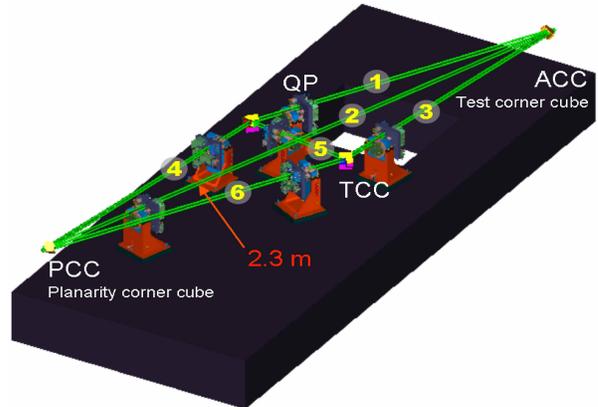


Fig 6. Diagram of the KITE testbed. The six metrology gauges interrogate 4 coplanar corner cube fiducials. They may be rotated and translated to simulate the motions of corner cubes mounted to SIM siderostats.

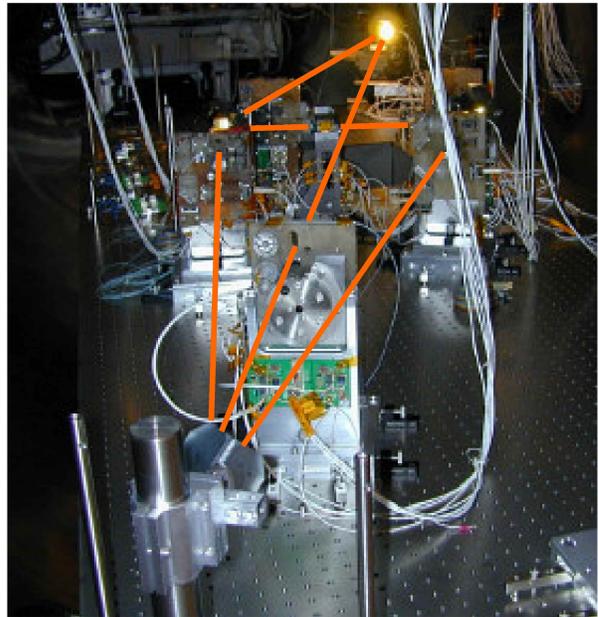


Fig.7. Photo of KITE testbed in vacuum chamber.

5.1 The KITE Metric

Fig. 8 diagrams KITE’s six metrology measurements. Since six measurements L_1, L_2, \dots, L_6 over-define the geometry, the longest measurement L_2 is treated as “truth” and can be compared with L_{2P} , the predicted length.

The KITE metric is the disagreement $\Delta \equiv L_2 - L_{2P}$ which should eventually be consistent with the SIM accuracy goals in Table 1.

Using the coordinate system defined in Fig. 8 the prediction L_{2P} can be calculated as follows:

$$\begin{aligned}
X_2 &= L_5, & Y_2 &= 0 \\
X_1 &= \frac{L_5^2 + L_3^2 - L_1^2}{2L_5}, & Y_3 &= (L_3 - X_1^2)^{1/2}, \\
X_3 &= \frac{L_5^2 + L_6^2 - L_4^2}{2L_5}, & Y_3 &= (L_6 - X_3^2)^{1/2}, \quad (3) \\
L_{2P} &= \left[(X_1 - X_3)^2 + (Y_1 - Y_3)^2 \right]^{1/2}.
\end{aligned}$$

Note that the measurements L_N are the sum of the *absolute* (measured once at the start of a run) and *relative* distances (monitored in real-time). Note also that the accuracies quoted below will be based on Δ 's divided by an appropriate scaling factor (typically ~ 1.4 to ~ 1.8) to apply to the context of SIM's metrology.

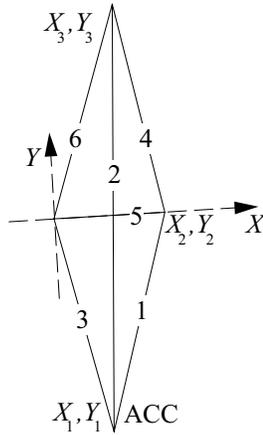


Fig. 8. Coordinate system for KITE metric.

5.2 KITE Results

KITE, as a representation of the SIM truss, was tested in two “astrometric observation” modes: narrow-angle (NA) and wide-angle (WA) as described in section 2. KITE’s articulated corner cube (ACC) moved by amounts similar to the SIM siderostat-mounted cube in these modes. The data reduction included the removal of linear drifts, taking advantage of the chopped astrometric observation schedule. Also, the data reduction includes the removal of a systematic linear error due to the corner cubes dihedral error and the imprecise co-location of vertices in the triple corner cubes.

For the higher accuracy NA mode, the typically observed metric Δ is currently about 20 pm RMS, higher than the SIM goal of 10 pm. For the WA test Δ is currently about 215 pm, again higher than the SIM goal.

KITE’s performance is expected to improve with the use of the next generation of metrology heads. These will have less drift, and are expected to accommodate

higher pointing dither frequencies for more accurate active alignment.

KITE’s electronics are also being upgraded to achieve lower drift and cyclic error.

6. CONCLUSION

SIM metrology has made significant strides. Table 3 summarizes the progress made thus far. It is anticipated that SIM’s goal will be reached in the near future.

In interpreting the numbers in Table 3, it should be remembered that the NA and WA modes include rotations of the fiducials to simulate SIM observations, and also include the data processing which removes linear drifts and linear field-dependent errors (section 2).

Table 3. Metrology accuracies as measured by the KITE testbed. All values are RMS and include linear error removal (see text). KITE metrology goals are close to, but not identical to SIM goals due to scaling factors.

	Achieved in 2004	KITE Goal
Accuracy, NA mode	20 pm	8 pm
Accuracy, NA mode without motions	2.8 pm	5 pm
Accuracy, WA mode	215 pm	140 pm

7. ACKNOWLEDGEMENT

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